

Dear Researchers & MSc students,

Chemical Engineering School of The University of Adelaide opens three PhD positions in the area of transport phenomena in porous media. The industrial and environmental applications include CO<sub>2</sub> and hydrogen storage, contamination of aquifers, well stimulation, and Enhanced Oil Recovery. However, the *focus of the work is on applied mathematics*. The activities include *exact and asymptotic solutions of non-linear partial differential equations*.

MSc in applied or pure mathematics, or in theoretical physics, is required. Publications would be a bonus for a candidate. The exceptional cases of MSc in mechanical, environmental, civil, petroleum, or chemical engineering with high mathematical background will be considered.

Please send your CV in English with the list of publications to [pavel.bedrikovetski@adelaide.edu.au](mailto:pavel.bedrikovetski@adelaide.edu.au). To see the recent publications of our group, please look into Bedrikovetsky in Google Scholar. The deadline for application is 01/11/2024.

Sincerely  
Pavel

## Stable Unique Riemann Solution For 2x2 Hyperbolic System

Multiple discontinuous solutions of conservation law systems is a well-known phenomenon. Selection of unique solution has been performed by either stability criteria or asymptotic vanishing dissipation method. Recently developed splitting mapping and the asymptotic method of matched singular first-order expansions allow deriving unique solutions of several Riemann problems. One of those relates to in situ storage of CO<sub>2</sub> and hydrogen in geological formations, which is a top priority in Australian energy sector.

The scope comprises derivation of unique Riemann solution for 2x2 hyperbolic system stable with respect to vanishing diffusion and capillary pressure. The topological aspect included description of the phenomenon in terms of classification of singular points of smooth manifolds. The industrial application includes using the Riemann solution in 3D commercial stream-line reservoir simulator.

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Borazjani, S., Roberts, A.J. and Bedrikovetsky, P., 2016. Splitting in systems of PDEs for two-phase multicomponent flow in porous media. *Applied Mathematics Letters*, 53, pp.25-32.

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